

# Synchronization in cortical neural networks

## – results, techniques and tools

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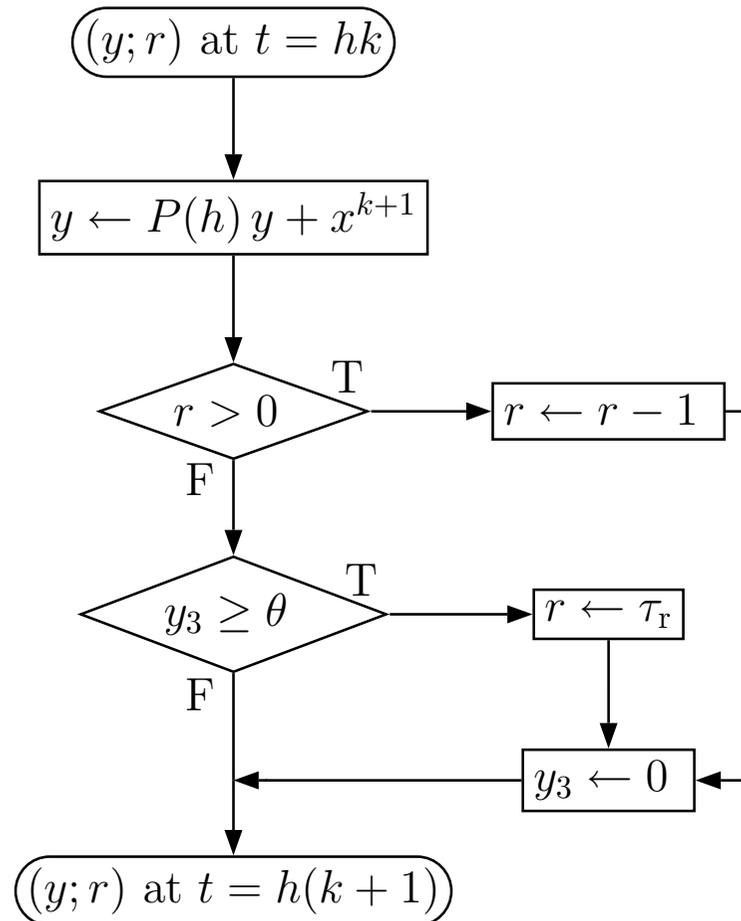
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# Overview

- Wednesday
  1. Feed-forward subnetworks in the cortex
  2. Parameters and variability of the synchronization dynamics
- Thursday
  3. Stability in recurrent cortical networks
  4. Integration of pulse-coupled neural networks
- Friday
  5. Simulation of realistic network structures by distributed computing

## Reminder: Single neuron simulation scheme



- state vector  $(\mathbf{y}; r)$
- $\mathbf{y}$ , subthreshold dynamics
- $r$ , time since last spike
- here,  $y_3$  membrane potential
- integration time step  $h$
- $P$  propagator
- input arriving at time  $h(k + 1)$

- ⇒
- spike times restricted to time grid (can be relaxed)
  - causality requires minimal delay  $h$

Diesmann et al. (2001) Neurocomput. **38–40**:565–571

## Reminder: Exact Integration

Thus, the system

$$\dot{\mathbf{y}} = \mathbf{A}\mathbf{y} = \begin{bmatrix} -\frac{1}{\tau_\alpha} & 0 & 0 \\ 1 & -\frac{1}{\tau_\alpha} & 0 \\ 0 & \frac{1}{C} & -\frac{1}{\tau_m} \end{bmatrix} \mathbf{y}, \quad \mathbf{y}(0) = \begin{bmatrix} \widehat{v} \frac{e}{\tau_\alpha} \\ 0 \\ 0 \end{bmatrix}$$

generates a PSP for initial condition  $\mathbf{y}(0)$ .

The exact solution of this system is given by

$$\mathbf{y}(t) = e^{\mathbf{A}t} \mathbf{y}(0),$$

where  $e^{\mathbf{A}t}$  denotes the **matrix exponential**

(think of power series  $e^{\mathbf{A}t} = \mathbf{1} + (\mathbf{A}t) + \frac{1}{2} (\mathbf{A}t)^2 + \frac{1}{6} (\mathbf{A}t)^3 + \dots$ ).

⇒ On the time grid  $\mathbf{y}^k = \mathbf{y}(kh)$  we can write

$$\mathbf{y}^{k+1} = e^{\mathbf{A}h} \mathbf{y}^k + \mathbf{x}^{k+1},$$

where  $\mathbf{x}^{k+1}$  is the initial condition for PSPs elicited at time  $(k+1)h$ .

# Simulation of realistic network structures by distributed computing

- Representation of network structure
- Update scheme
- Communication
- Random numbers
- Performance
- Summary

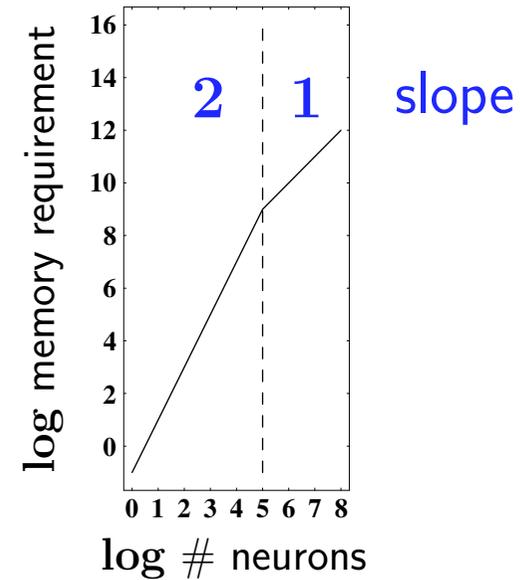
A. Morrison, C. Mehring, T. Geisel, A. Aertsen, & M. Diesmann (2005) *Advancing the boundaries of high connectivity network simulation with distributed computing*. *Neural Computation*, in press  
(all figures, references to textbooks and original work)

# Realistic local cortical networks

- connectivity  $c = 0.1$
  - synapses per neuron =  $10^4$
- ⇒ minimal network size =  $10^5$

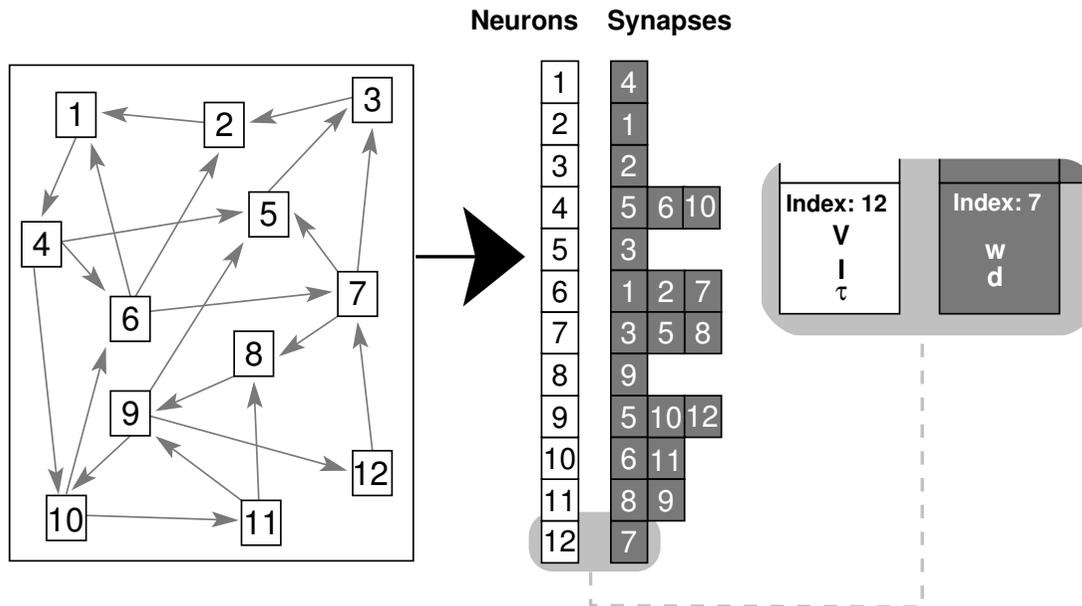
network of  $N = 10^5$  neurons  
considered elementary unit of cortex  
corresponding to  $1 \text{ mm}^3$

$$\text{total number of synapses} = (cN) \cdot N$$

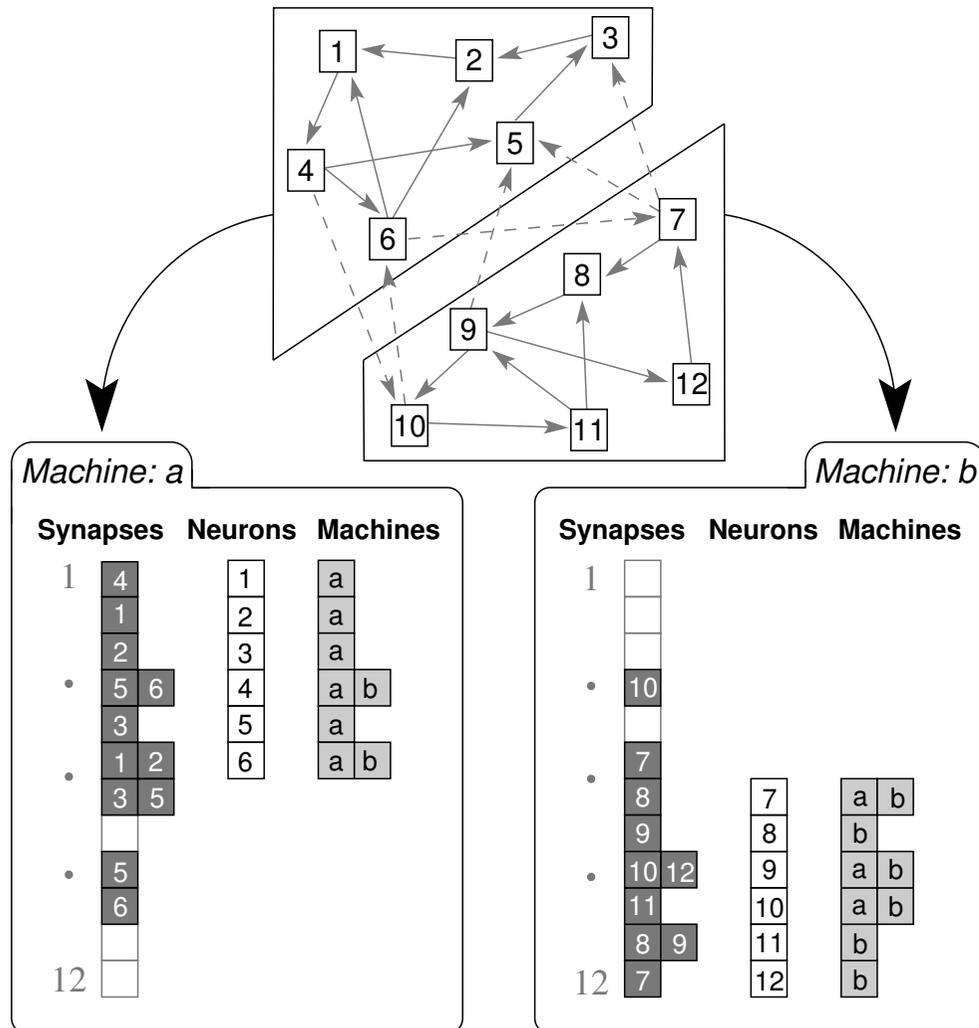


⇒ possible

# Representation of network structure: Serial

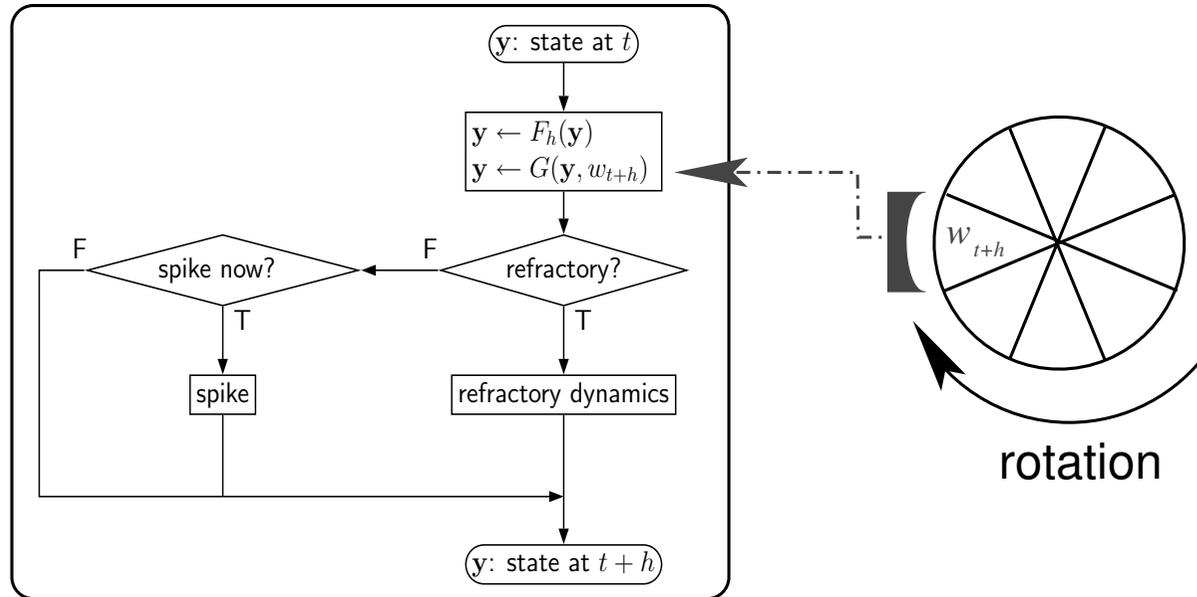


# Representation of network structure: Distributed



- modulo operation distributes neurons
  - $i \rightarrow j$ :
    - one target list for  $i$  on each machine
    - synapse stored on machine owning  $j$
  - compressed target lists
  - list of target machines for each neuron
- 
- crude load balancing
  - wiring is a parallelizable task

# Neuron update



- “looped tape device” buffers incoming events
- position determined by delay
- no central queue required
- maximal delay determines length of tape
- minimal delay is  $h$
- IVP 1-d  $\rightarrow$  tape 1-d

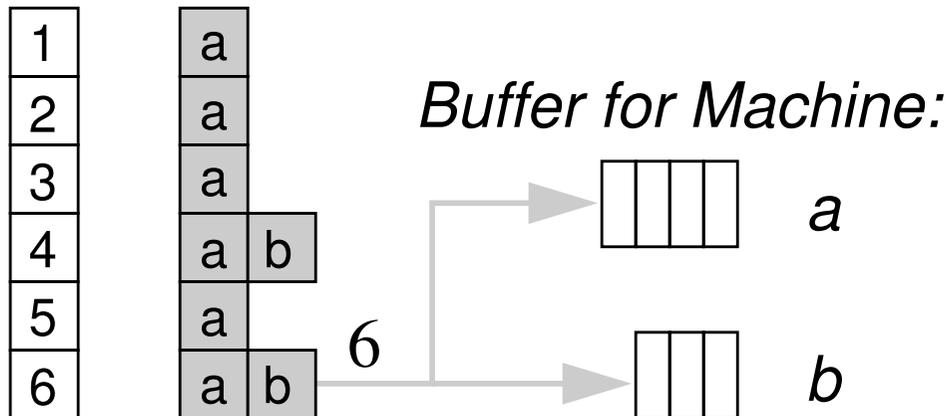
Time-driven or event-driven? –a hybrid approach to simulation

- input events to neurons are frequent: time-driven algorithm
- events at individual synapses are rare: event driven component

# Buffering of events prior to communication

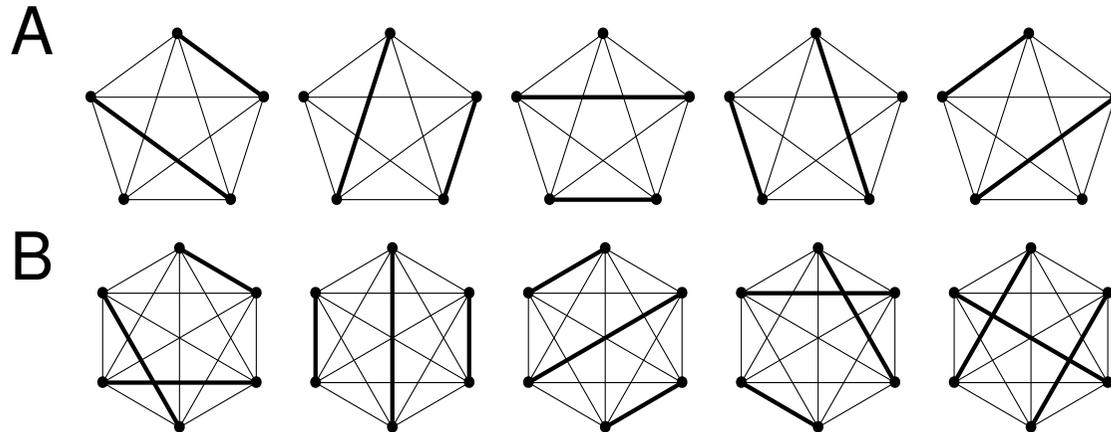
*Machine: a*

**Neurons Machines**



- communication only required in intervals of the minimal delay
- communication load independent of computation step size  $h$
- events sent only to machines where needed

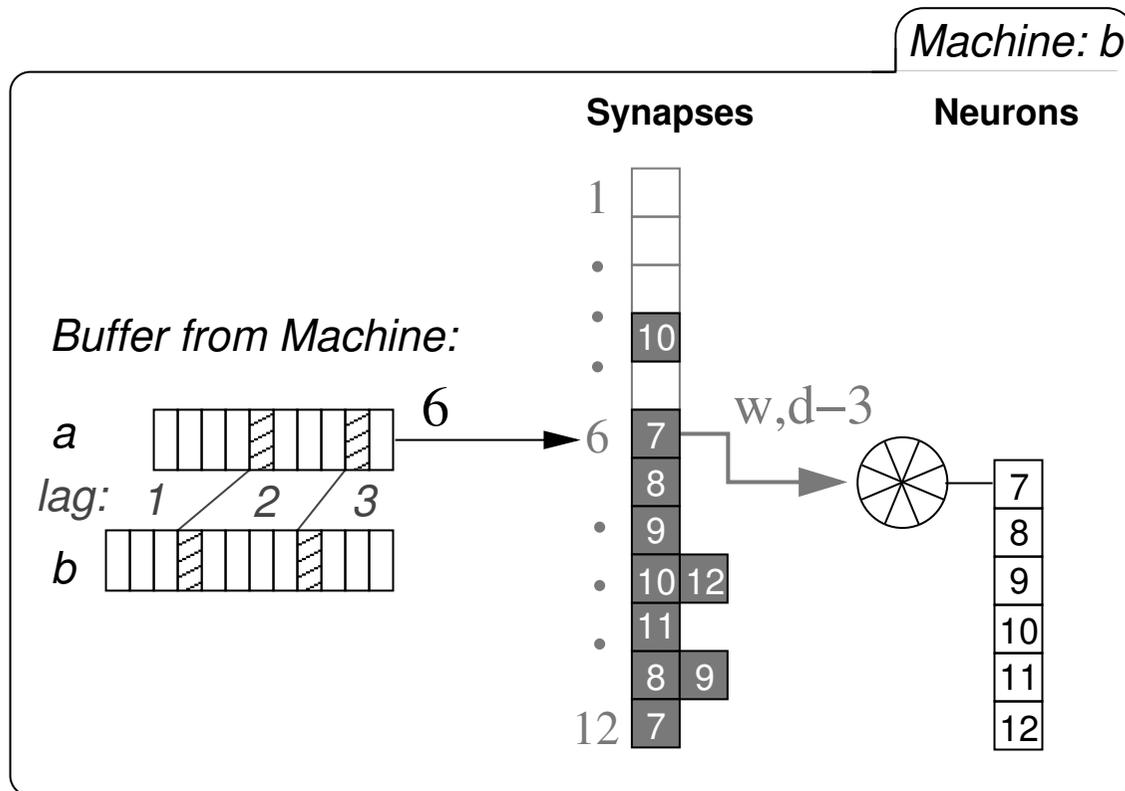
# Complete pairwise exchange (CPEX)



- blocking MPI Send and Receive
- communication is parallel

- equivalent to an edge coloring problem (Tam & Wang, PDCS 2000, Las Vegas)
- edges with same color are parallel exchanges not causing deadlock
- number of machines  $m$  odd:  $m$  colors (steps)
- number of machines  $m$  even:  $m - 1$  colors (steps)

# Event delivery

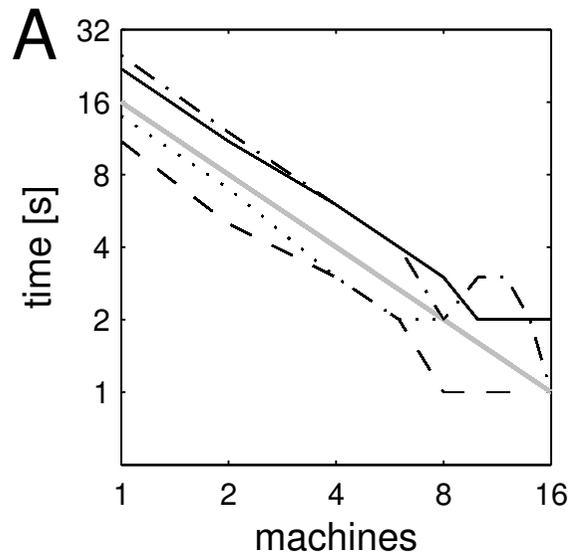


- received buffers are sequentially processed
- synapses activated according to received neuron indices
- markers indicate start of new time step

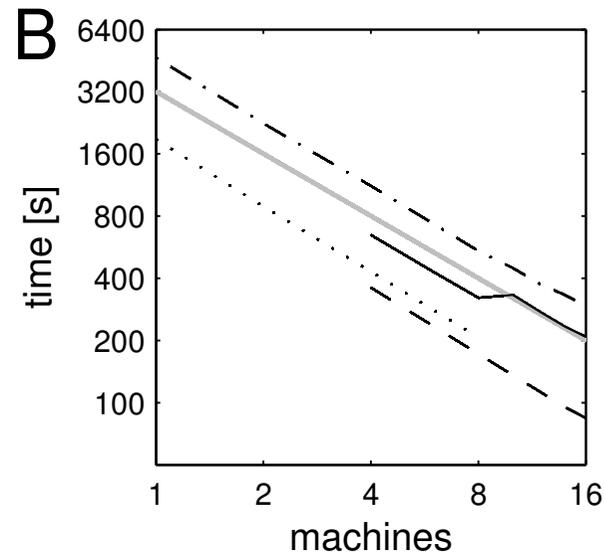
# Random numbers

- random number generators with independent trajectories for different seeds (Knuth, 1997)
- GNU Scientific Library ensures platform independence
- *pseudo processes provide independence of number of processors*

# Scalability of wiring



$10^4$  neurons



$10^5$  neurons

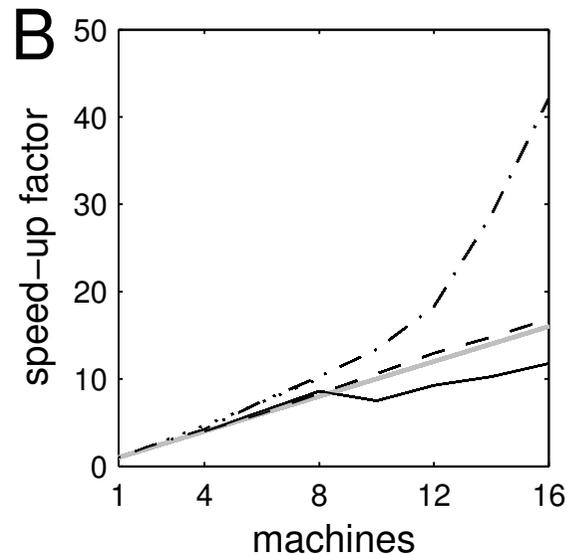
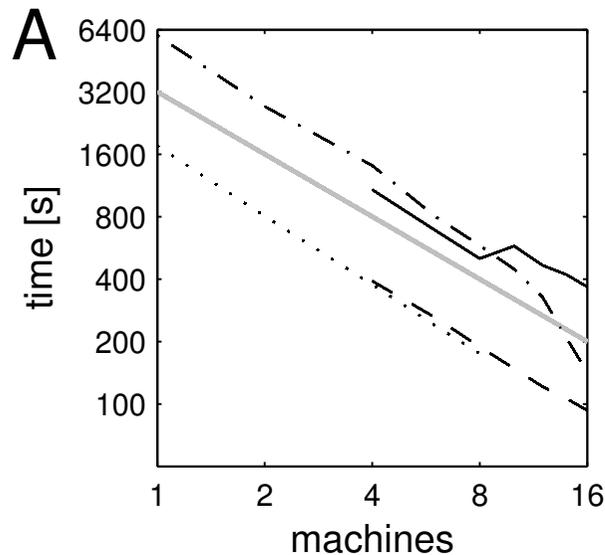
$$T(m) = T(1)/m$$

$$\log T(m) = \log T(1) - \log m$$

log-log plots are easier to interpret

- (solid) elderly PC:  $8 \times 2$ , Pentium 0.8 GHz, 100 MBit Ethernet
- (dashed) recent PC:  $20 \times 2$ , Xeon 2.8 GHz, Dolphin/Scali
- (dash-dotted) Compaq GS160: 16, Alpha 0.7 GHz
- (dotted) Compaq GS1280: 8, Alpha 1.15 GHz

# Scalability of simulation time



$$T(m) = T(1)/m$$

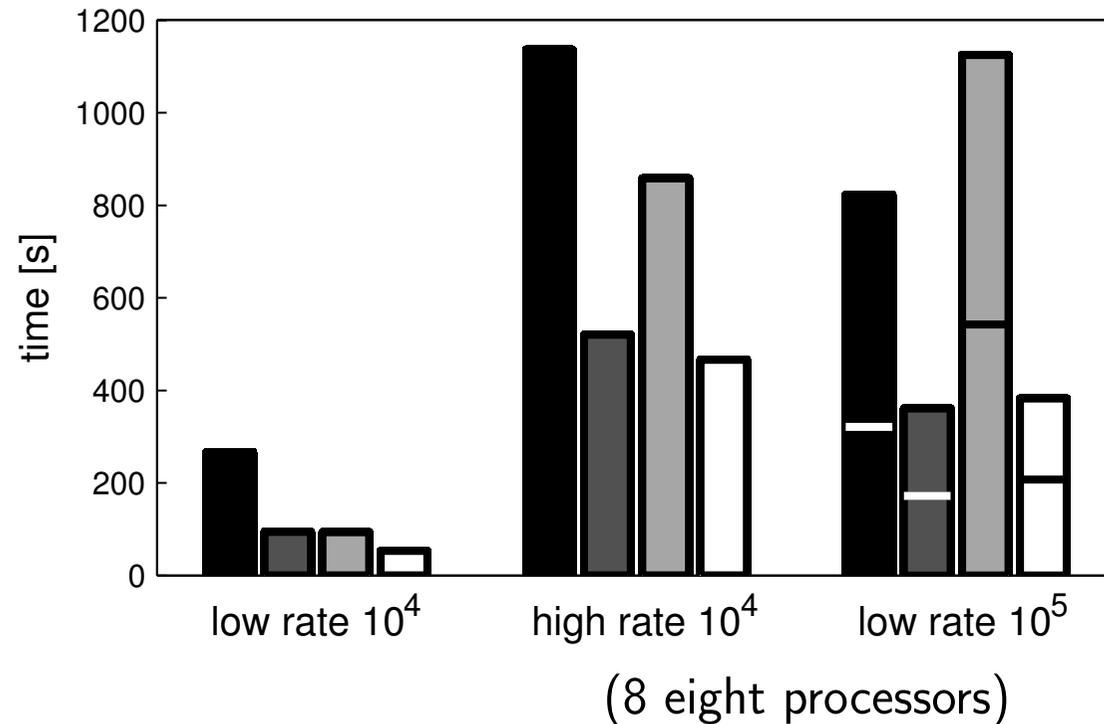
$$S(m) = T(1)/T(m) \\ = m$$

⇒ speed-up  $S(m)$

- linear scaling
- supra-linear (cache)
- limited by memory bandwidth

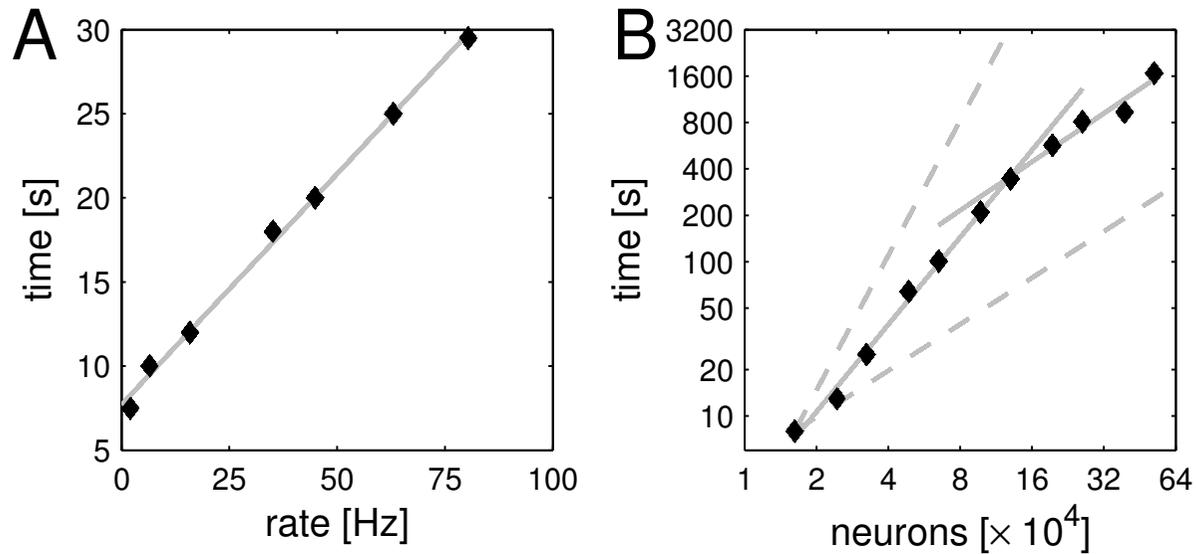
- (solid) elderly PC:  $8 \times 2$ , Pentium 0.8 GHz, 100 MBit Ethernet
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- (dash-dotted) Compaq GS160: 16, Alpha 0.7 GHz
- (dotted) Compaq GS1280: 8, Alpha 1.15 GHz

# Comparison of computer architectures



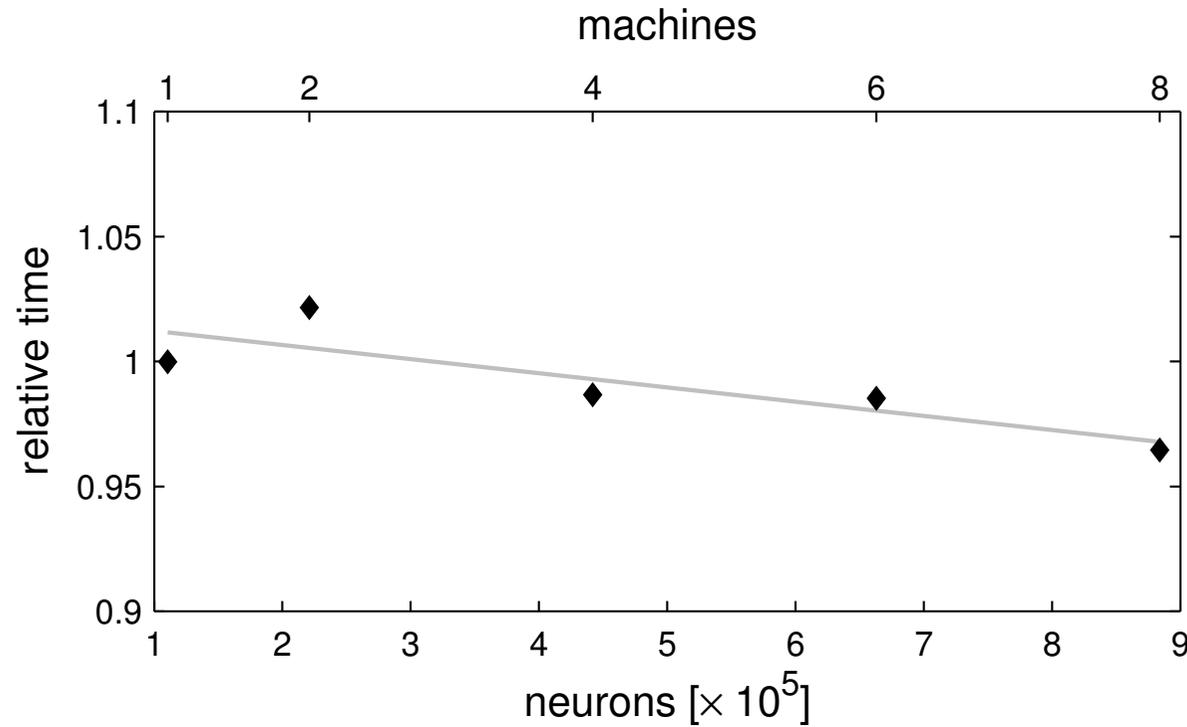
- (black) elderly PC:  $8 \times 2$ , Pentium 0.8 GHz, 100 MBit Ethernet
- (dark gray) recent PC:  $20 \times 2$ , Xeon 2.8 GHz, Dolphin/Scali
- (light gray) Compaq GS160: 16, Alpha 0.7 GHz
- (white) Compaq GS1280: 8, Alpha 1.15 GHz

# Scalability with respect to activity and network size



- linear in spike rate
- slope 1.88 with quadratically increasing number of synapses until  $> 10^5$  (1.05)

# Scalability with respect to problem size



$$T(m) = [T(1) \cdot m] / m$$

$$S(m) = T(1) / T(m) \\ = 1$$

⇒ scaled speed-up  $S(m)$

- GS1280
- measured slope  $-0.0057$

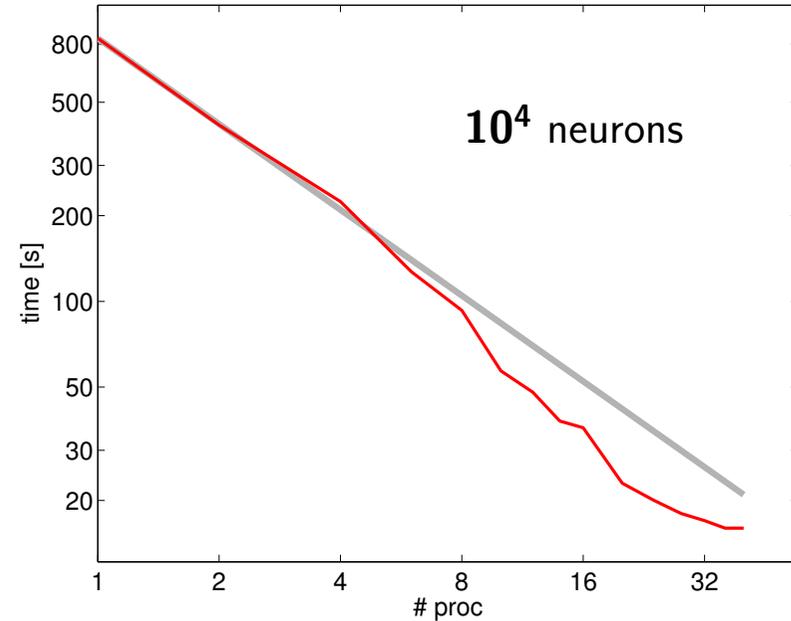
# More processors

- not limited by communication
- profits from cache memory
- non-deterministic algorithms
- limited by memory bandwidth

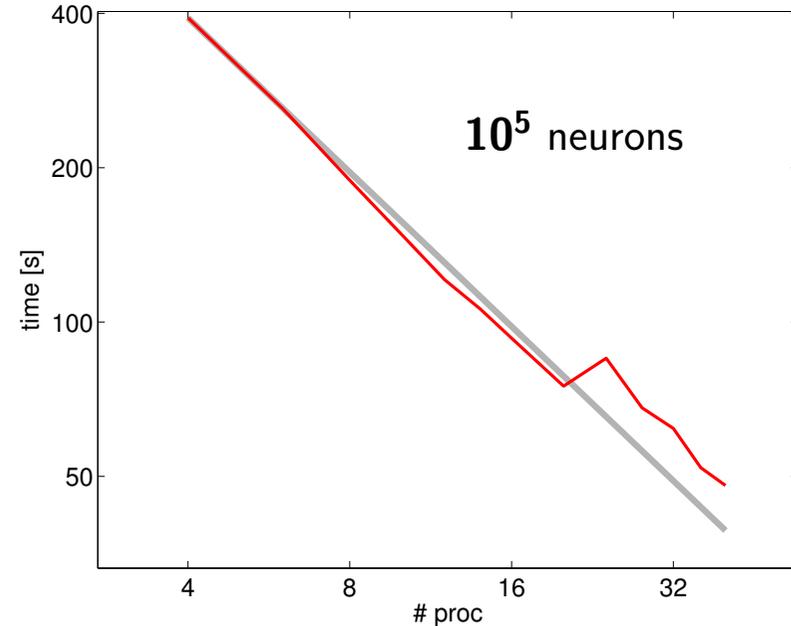
- permits quasi-interactive style of working

here: recent PC:  $20 \times 2$ , Xeon 2.8 GHz, Dolphin/Scali

basis simulation: simulation time against number of processors

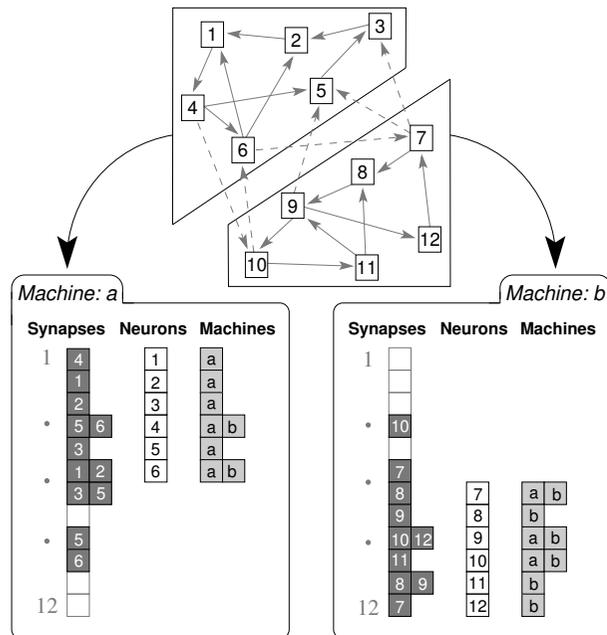


huge simulation: simulation time against number of processors



# Organization

## Distributed development of simulation tools



since 2001

Institute of Biology III  
Albert-Ludwigs-University

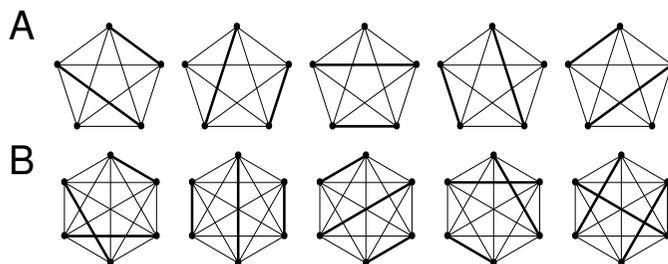
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Max-Planck-Institute for Fluid Dynamics

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- distributed and cache optimized data structures



- efficient communication algorithms

M. Diesmann & M.-O. Gewaltig (2002) *NEST; An environment for neural systems simulations*, GWDG-Bericht **58**:43–70

# Summary

- Simulation on a time grid
- Minimal delay of  $h$  required by causality
- Partial target lists local to the machine owning the targets
- Compression of target lists
- Frequency of communication steps independent of computation step size
- Reproducible simulations by *pseudo processes*
- Complete pairwise exchange with blocking communication
- Linear speed-up
- Quasi-interactive: Qualitatively new style of working
- Scalable to larger problems

# Thanks

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