



Nuclei as **open** quantum many body systems

Witold Nazarewicz (Tennessee/Warsaw)

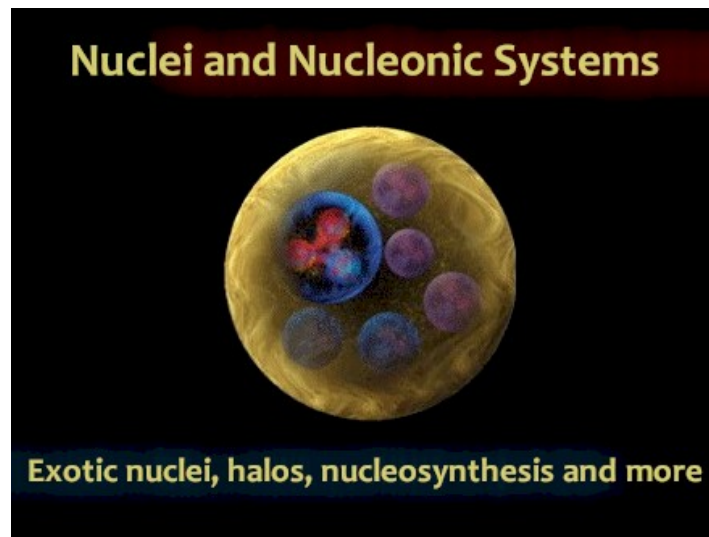
20th Chris Engelbrecht Summer School in Theoretical Physics

19 – 28 January 2009

National Institute for Theoretical Physics at Stellenbosch

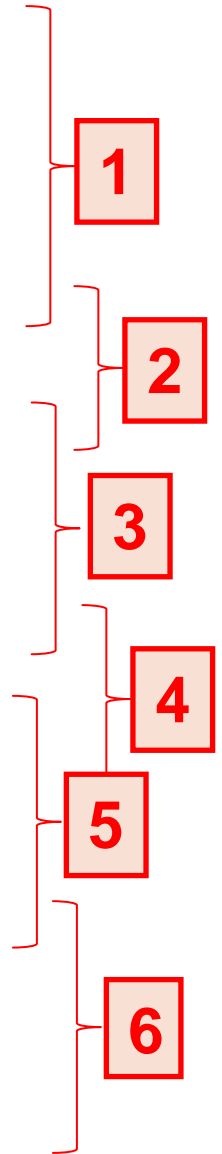
Institute for Advanced Study,

Stellenbosch, Western Cape, South Africa



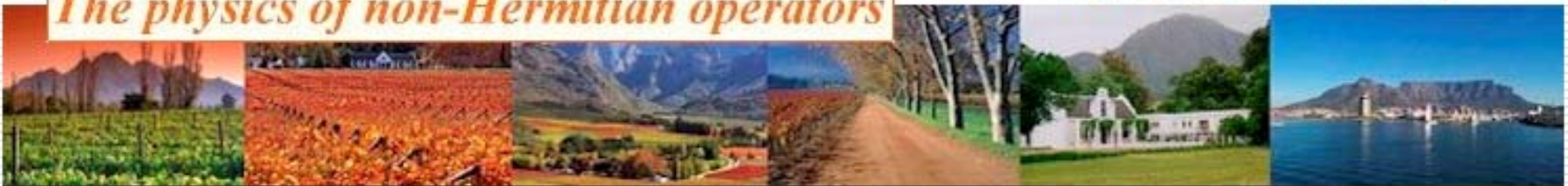
Rough Outline

- Introduction: nuclei as open systems
- Territory: nuclear landscape and the limits of nuclear existence
- Phenomena related to the openness
 - Coupling between structure and reactions
- Recent experimental highlights
- General comments on nuclear many-body theory
- Simple concepts
- Theoretical frameworks
 - Real-energy quantum mechanics (Hilbert Space)
 - Mean field perspective
 - Continuum shell model
 - Complex-energy quantum mechanics (Rigged Hilbert Space)
 - Resonant-state expansions
 - Gamow Shell Model and Complex Scaling
- Typical applications
 - Weakly bound and unbound nuclei
 - Fission
 - Hot nuclei and continuum level density
 - Other many-body systems; interdisciplinary aspects
- Perspectives



The physics of non-Hermitian operators

The 4th International Workshop



Pseudo-Hermitian Hamiltonians in Quantum Physics IV



Last updated: 31 July 2006

WHERE: The Workshop was held at the University of Stellenbosch, Western Cape, South Africa

WHEN: November 23-25, 2005

Also see: [Workshop series home page](#)
[The 1st Workshop \(2003\)](#)
[The 2nd Workshop \(2004\)](#)
[The 3rd Workshop \(June 2005\)](#)
[The 5th and upcoming Workshop \(July 2006\)](#)

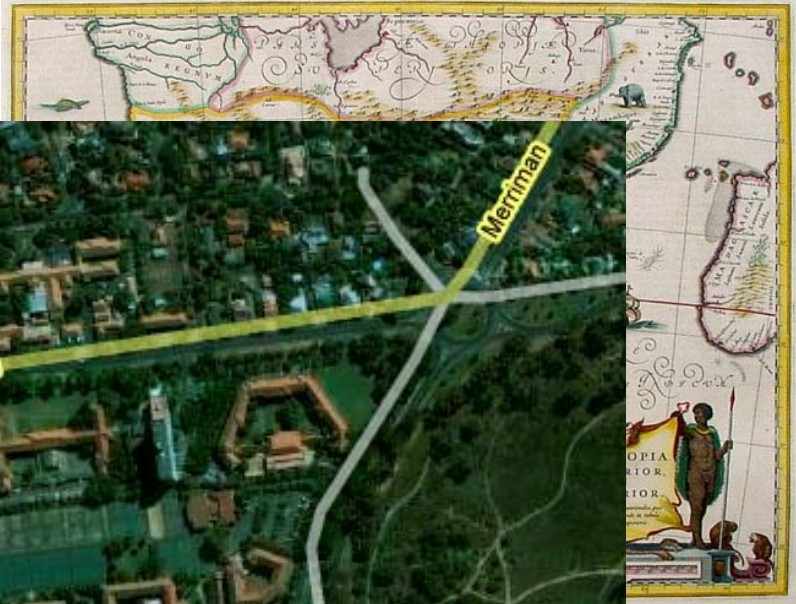
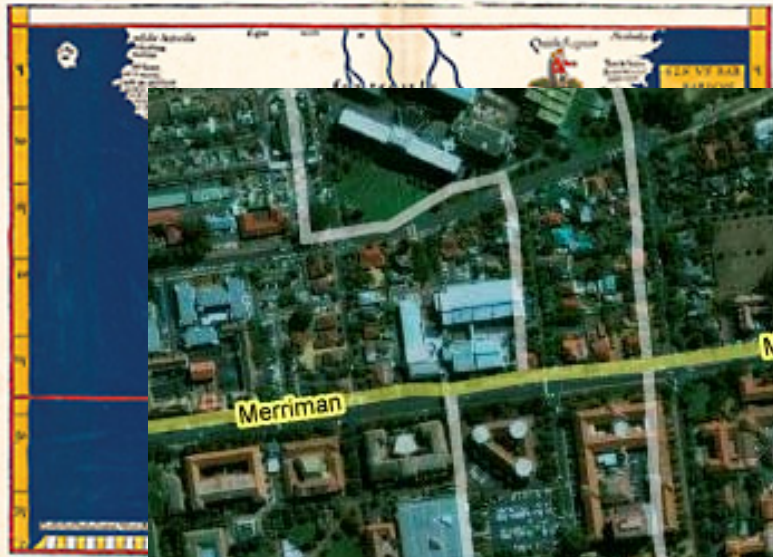
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Topics

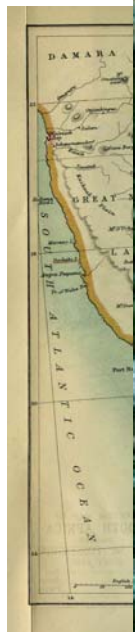
The scope of the conference:

- ALGEBRAIC, PERTURBATION AND NUMERICAL METHODS
- APPLICATIONS IN MAGNETOHYDRODYNAMICS ETC
- EFFECTIVE THEORIES IN MANY-BODY PROBLEMS
- EXCEPTIONAL POINTS
- FIELD THEORIES WITH CPT SYMMETRY
- KREIN SPACES AND RELATED RIGOROUS RESULTS
- QUASI-HERMITIAN MODELS IN QUANTUM MECHANICS
- RANDOM MATRIX MODELS AND NON-HERMITICITY IN STATISTICAL PHYSICS

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Ptole



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Introduction

Wikipedia:

An open quantum system is a quantum system which is found to be in interaction with an external quantum system, the environment. The open quantum system can be viewed as a distinguished part of a larger closed quantum system, the other part being the environment.

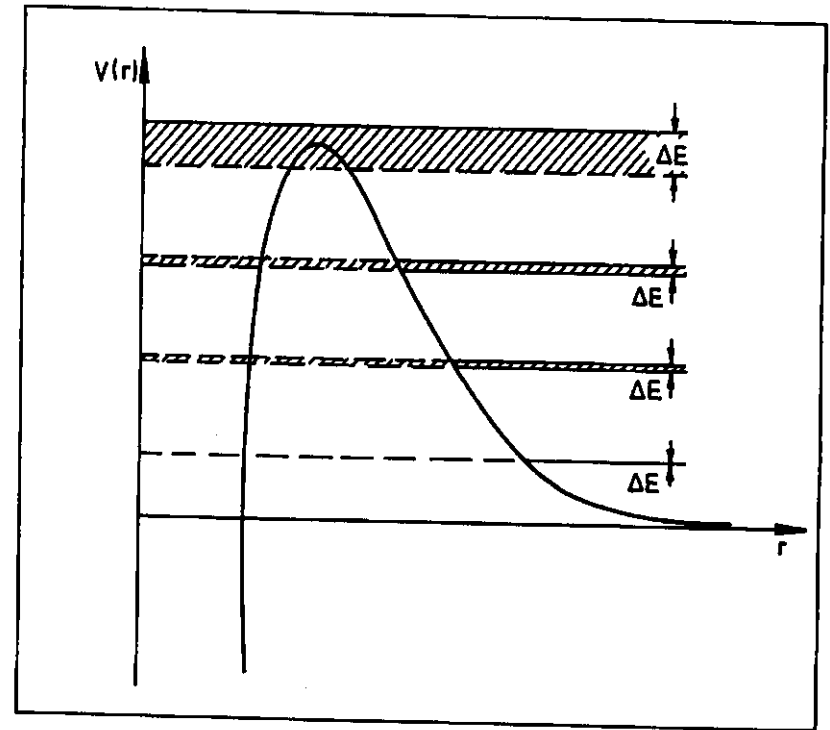
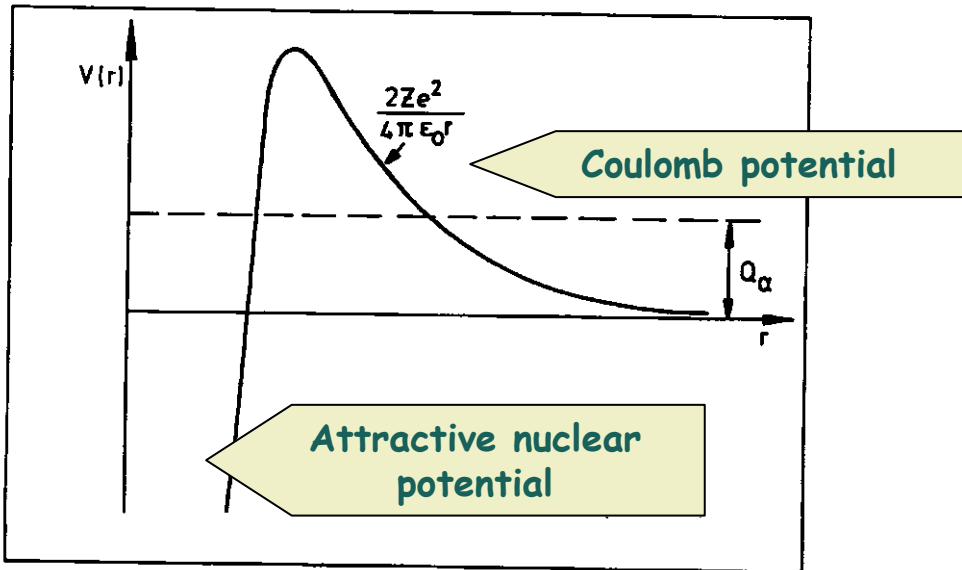
environment:

closed quantum system, the other part being the
can be viewed as a distinguished part of a larger
system, the environment. The open quantum system
is found to be in interaction with external quantum
whether degree of freedom, energy, matter,



Nuclear Decays

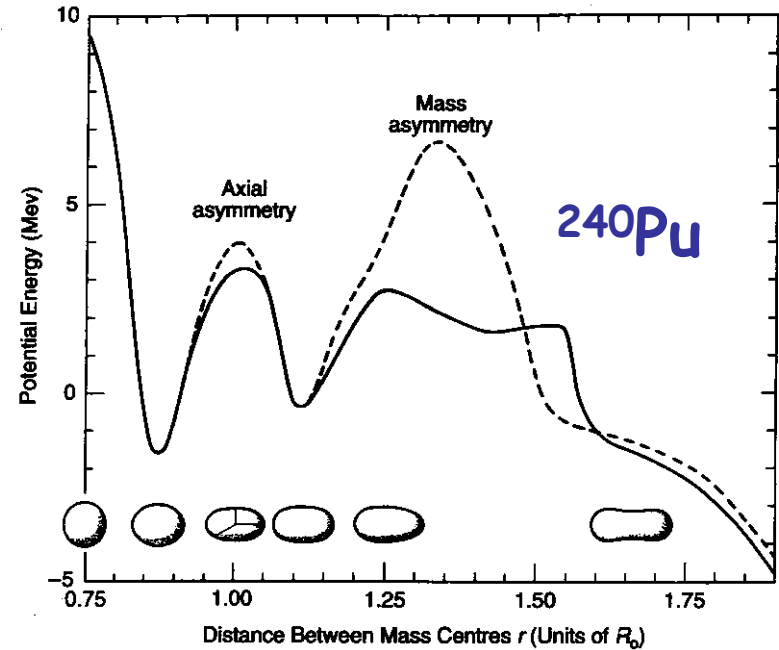
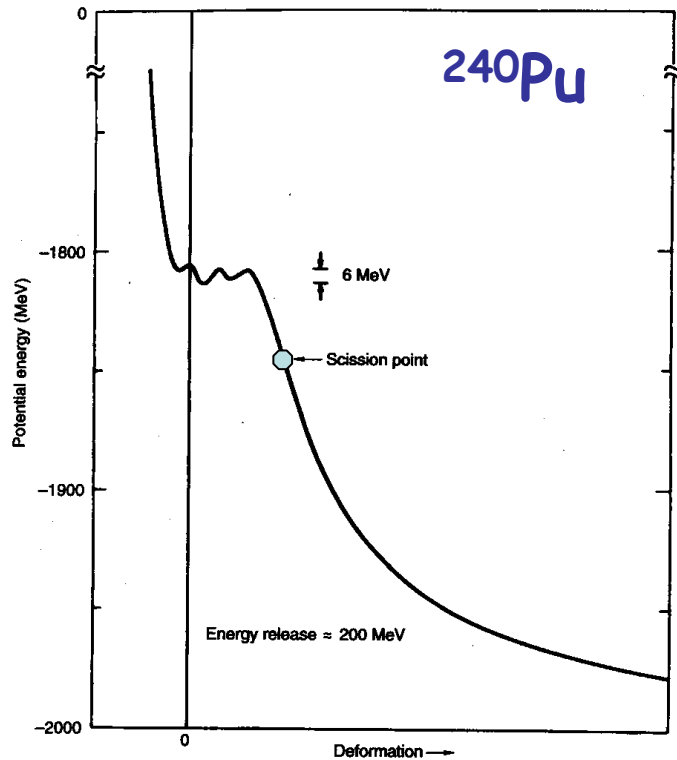
Alpha Decay



Gamow 1928

("pre-nuclear" era)

Spontaneous fission



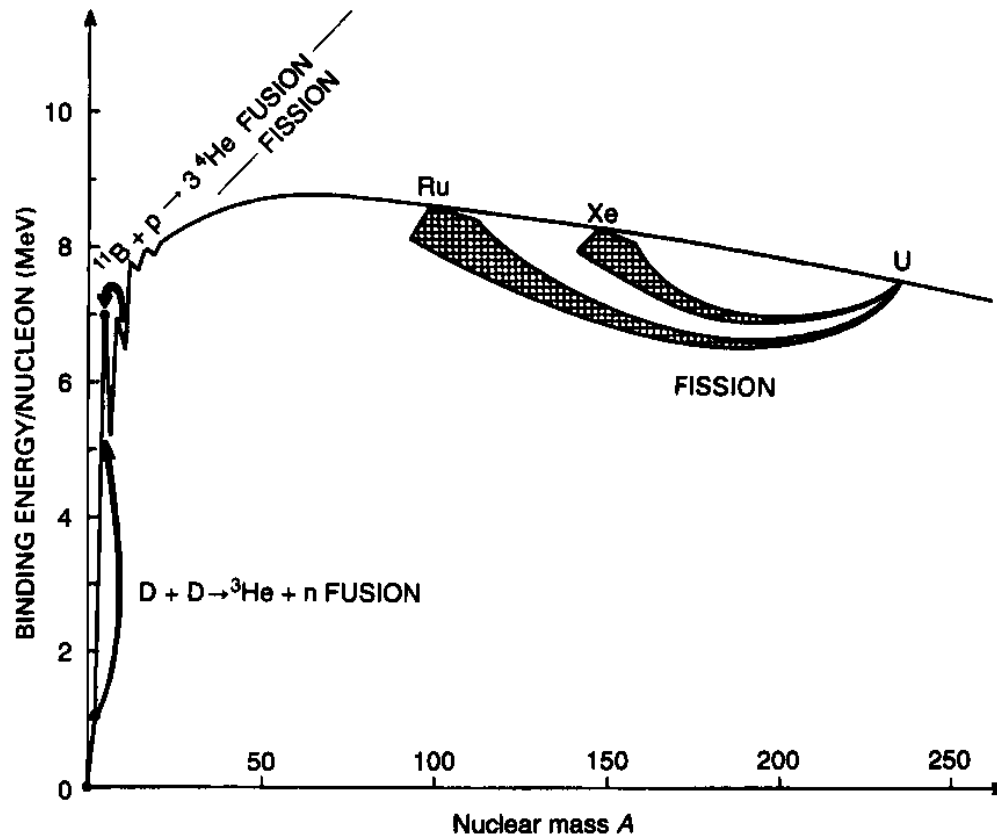
1938 - Hahn & Strassmann

1939 Meitner & Frisch

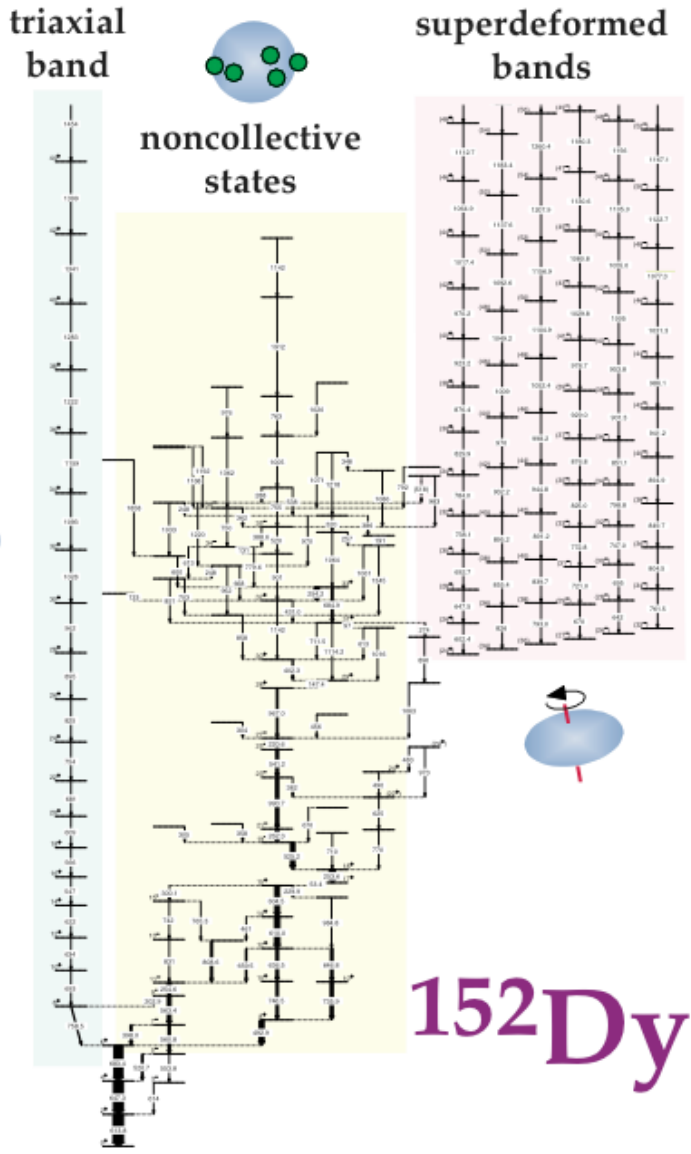
1939 Bohr & Wheeler

1940 Petrzhak & Flerov

- All elements heavier than $A=110-120$ are fission unstable!
- But... the fission process is unimportant for nuclei with $A < 230$. Why?



Coexistence of collective and noncollective motion

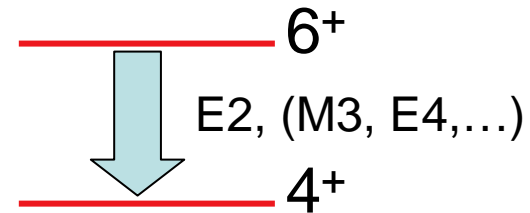


Electromagnetic Decay

Emission of a γ -ray is caused by the interaction of the nucleus with an external electromagnetic field

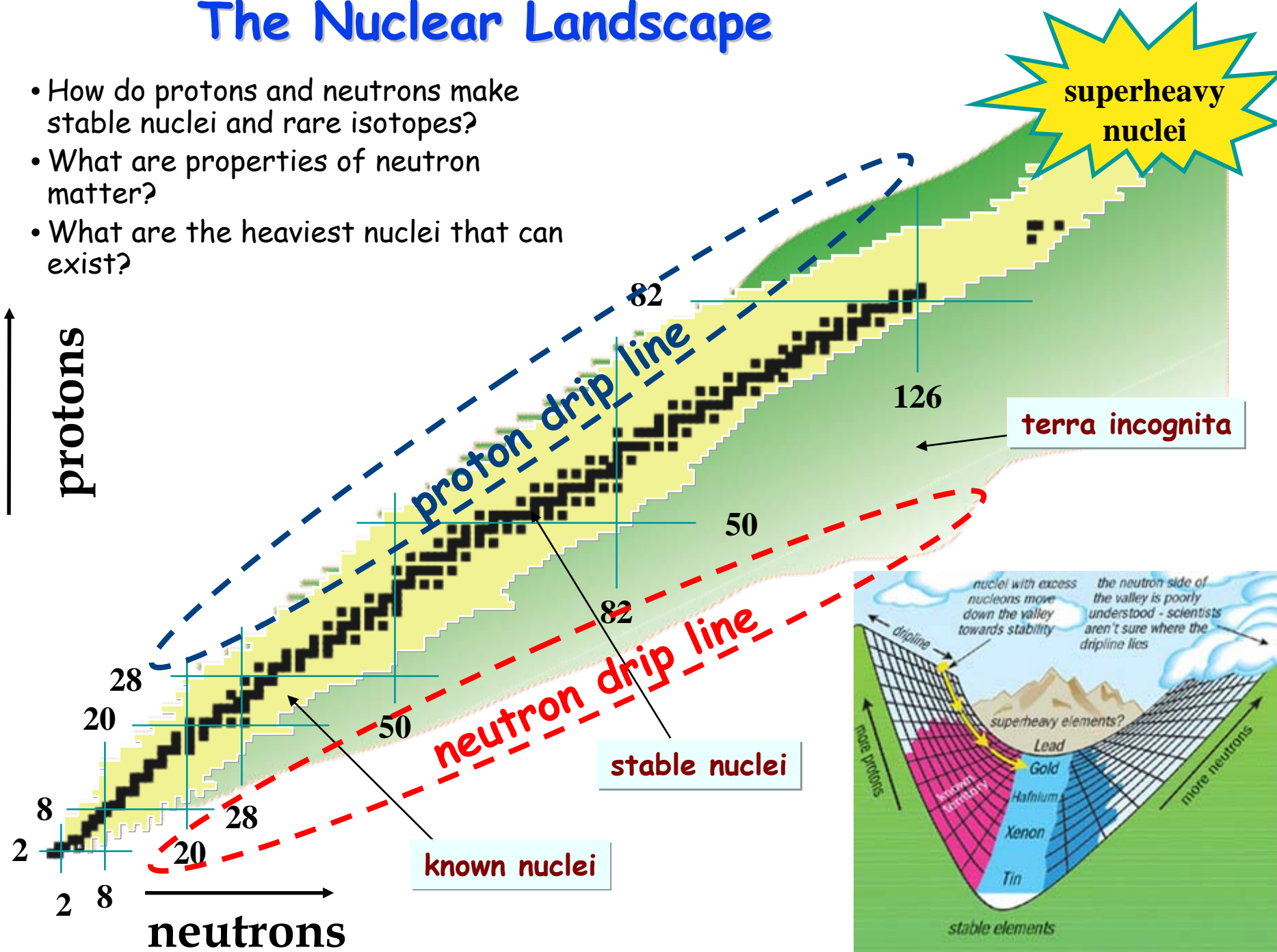
$$V = -\frac{1}{c} j_{\mu} A^{\mu}$$

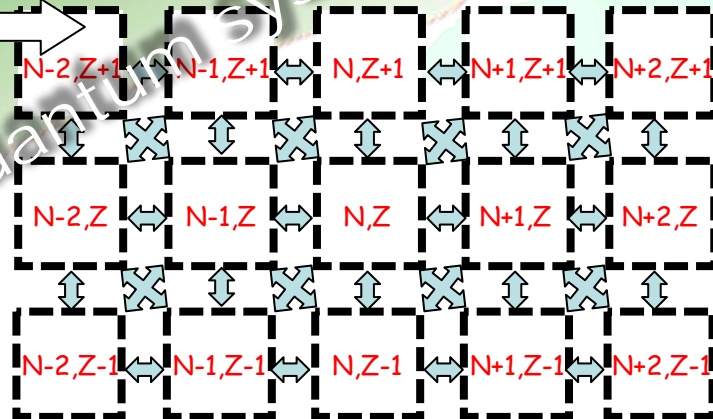
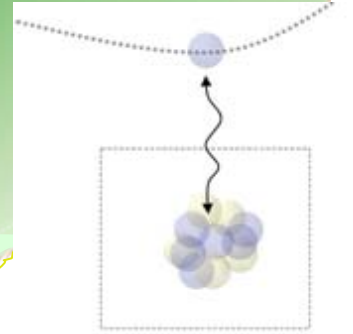
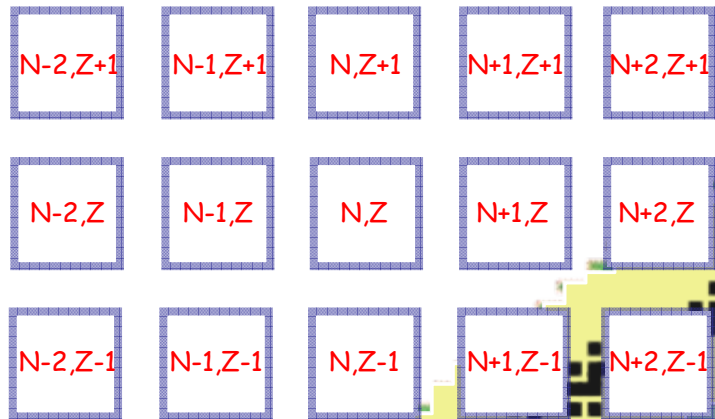
Nuclear current External EM field



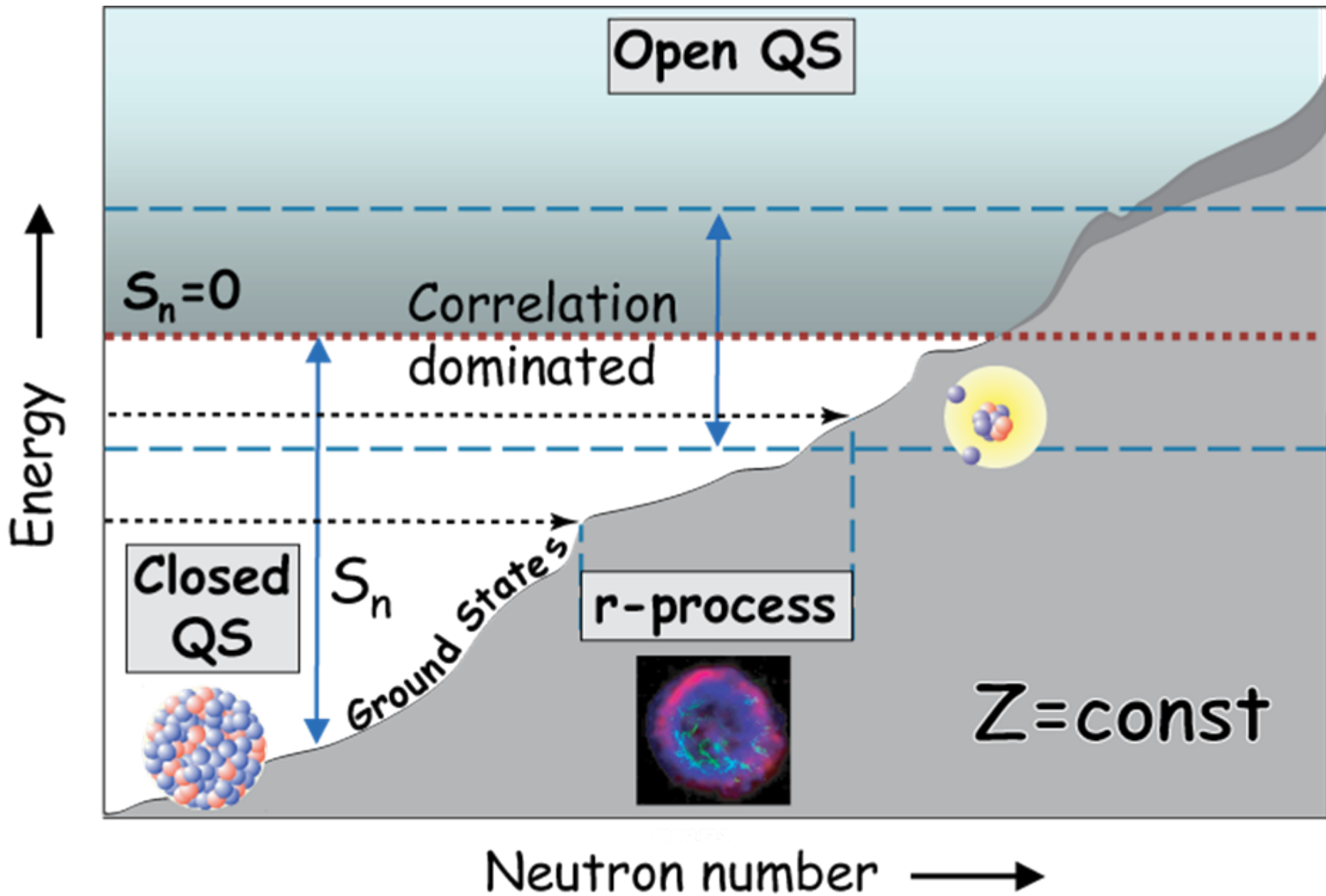
The Nuclear Landscape

- How do protons and neutrons make stable nuclei and rare isotopes?
- What are properties of neutron matter?
- What are the heaviest nuclei that can exist?





open quantum systems



Basic Equations

Time Dependent (Many Body) Schödinger Equation

$$i\hbar \frac{\partial \psi}{\partial t} = \hat{H} \psi$$

+ boundary conditions

Often impractical/impossible to solve but excellent starting point

Time Independent (Many Body) Schödinger Equation

$$\hat{H} \psi = E \psi$$

Box boundary conditions (w.f. vanishes at large distances)

Decaying boundary conditions

Incoming or capturing boundary conditions

Scattering boundary conditions

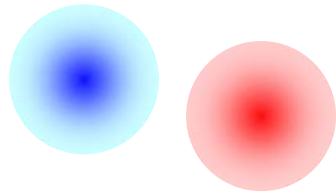
Absorbing boundary conditions

} choice
depends
on
physics
case

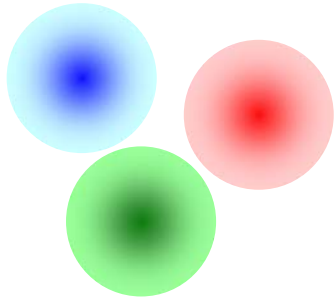
Phenomena related to the Openness

**Impact of scattering space
on structural properties**

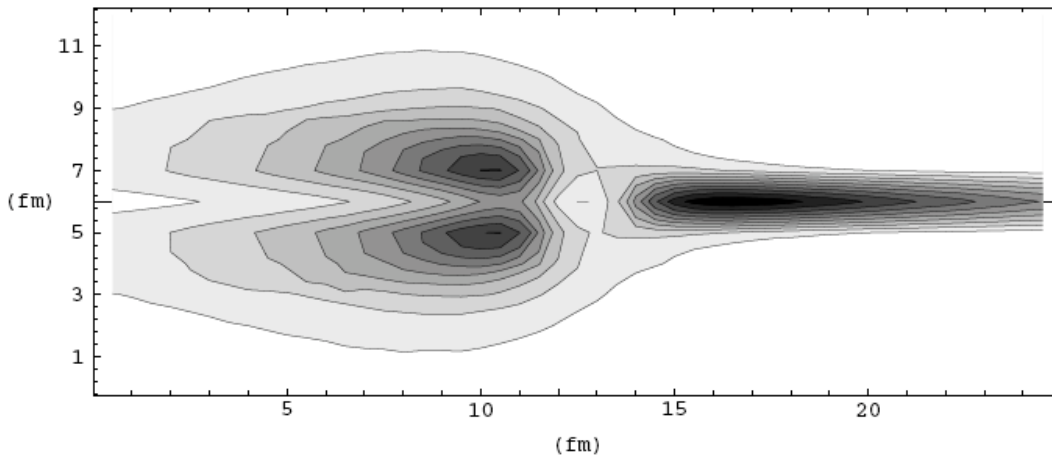
Halos



${}^2\text{H}$ (deuteron)
 $S_n = 2.2 \text{ MeV}$, $r_{np} = 4 \text{ fm}$



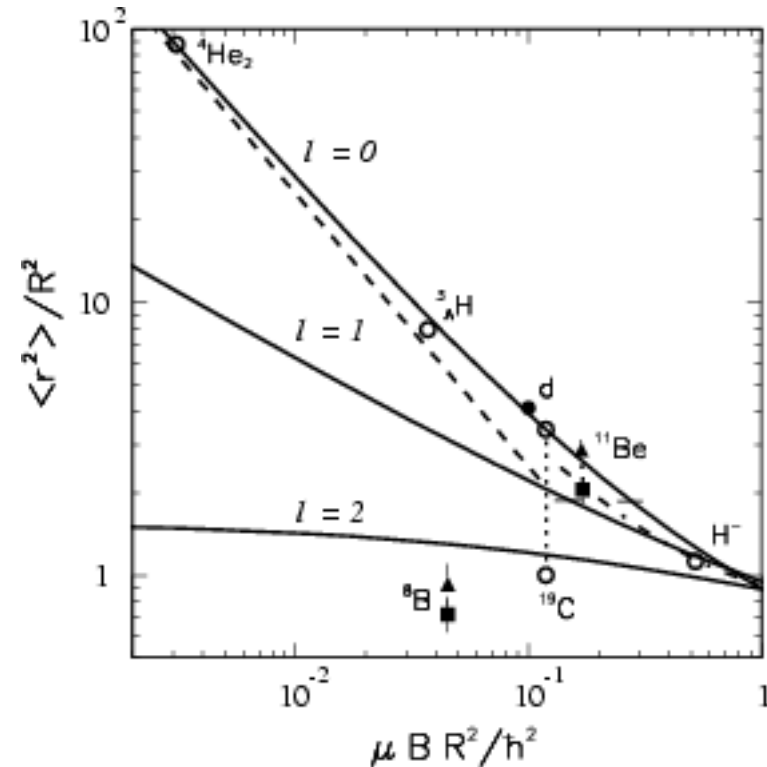
${}^3\text{H}_L$ (hypertriton)
 $S_\Lambda = 0.08 \text{ MeV}$



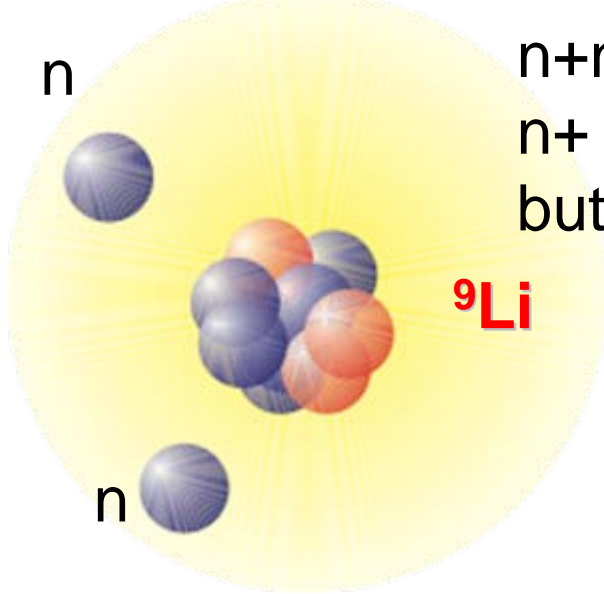
Cobis, Jensen, Fedorov
 J. Phys. G23, 401 (1997)

Riisager, Fedorov, Jensen
 Europhys. Lett. 49, 547 (2000)

${}^4\text{He}_2$ (atomic helium dimer)
 $S = 0.13 \text{ } \mu\text{eV}$, $r = 100 \text{ } \text{Å}$

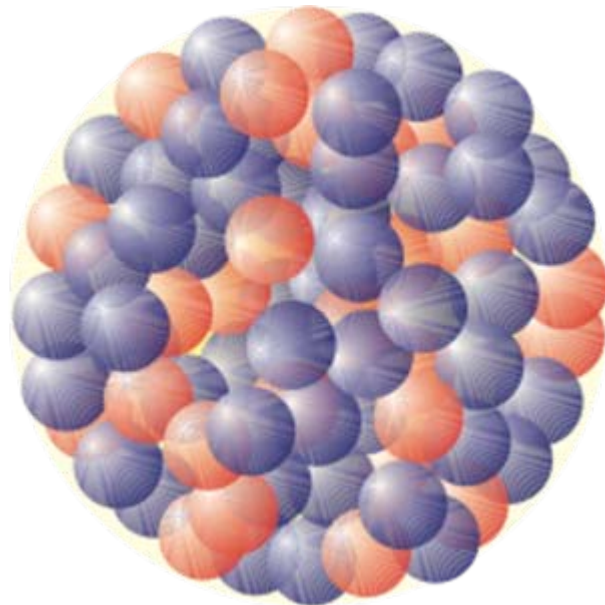


^{11}Li : Borromean halo nucleus
 $Z=3, N=8$



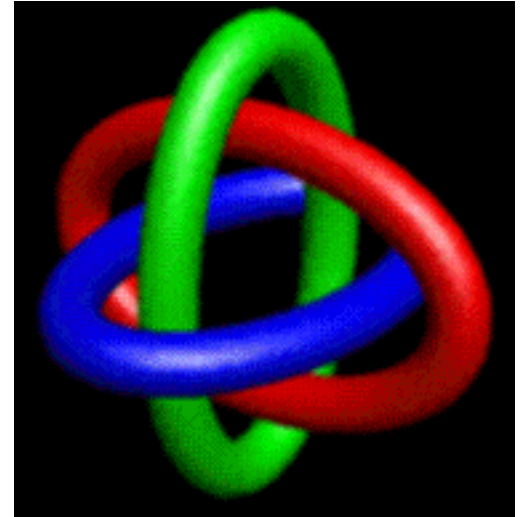
$n+n$ is unbound
 $n+{}^9\text{Li}$ is unbound
but $n+n+{}^9\text{Li}$ is bound !

← 0.00000000000014 cm →



**^{208}Pb : well bound
heavy nucleus**
 $Z=82, N=126$

**The Borromean
Rings**

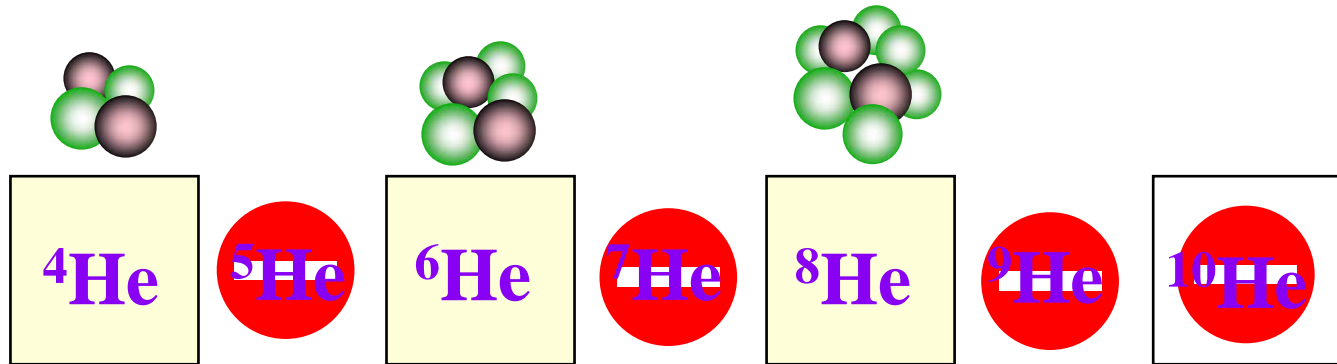


Neutron Drip line nuclei

HUGE

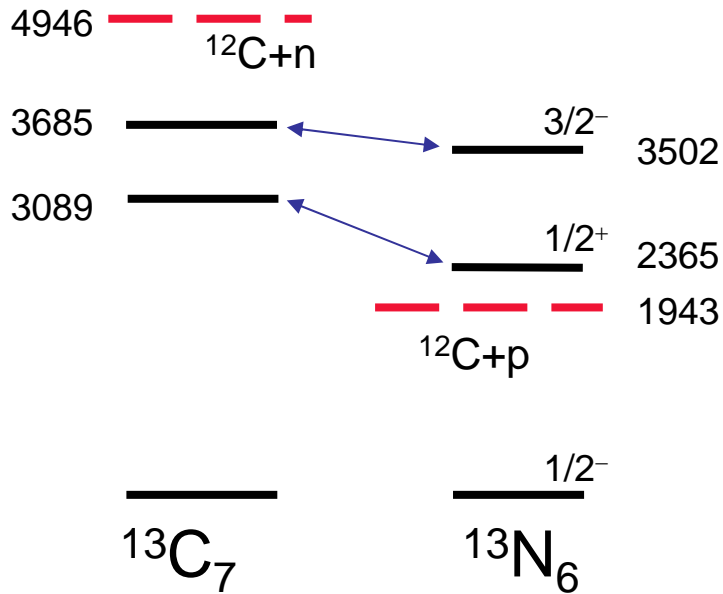
Diffused

PAIRED

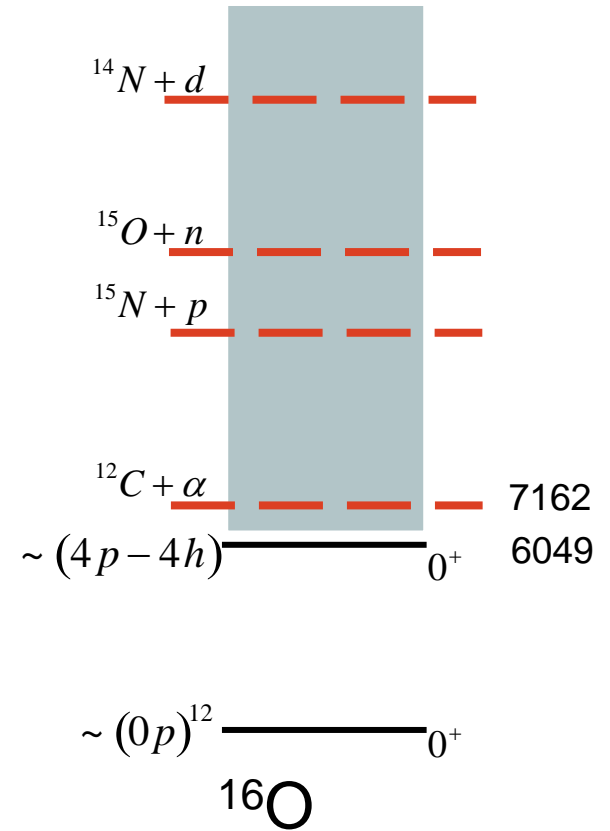


Environment: continuum of decay channels

Thomas-Ehrmann effect

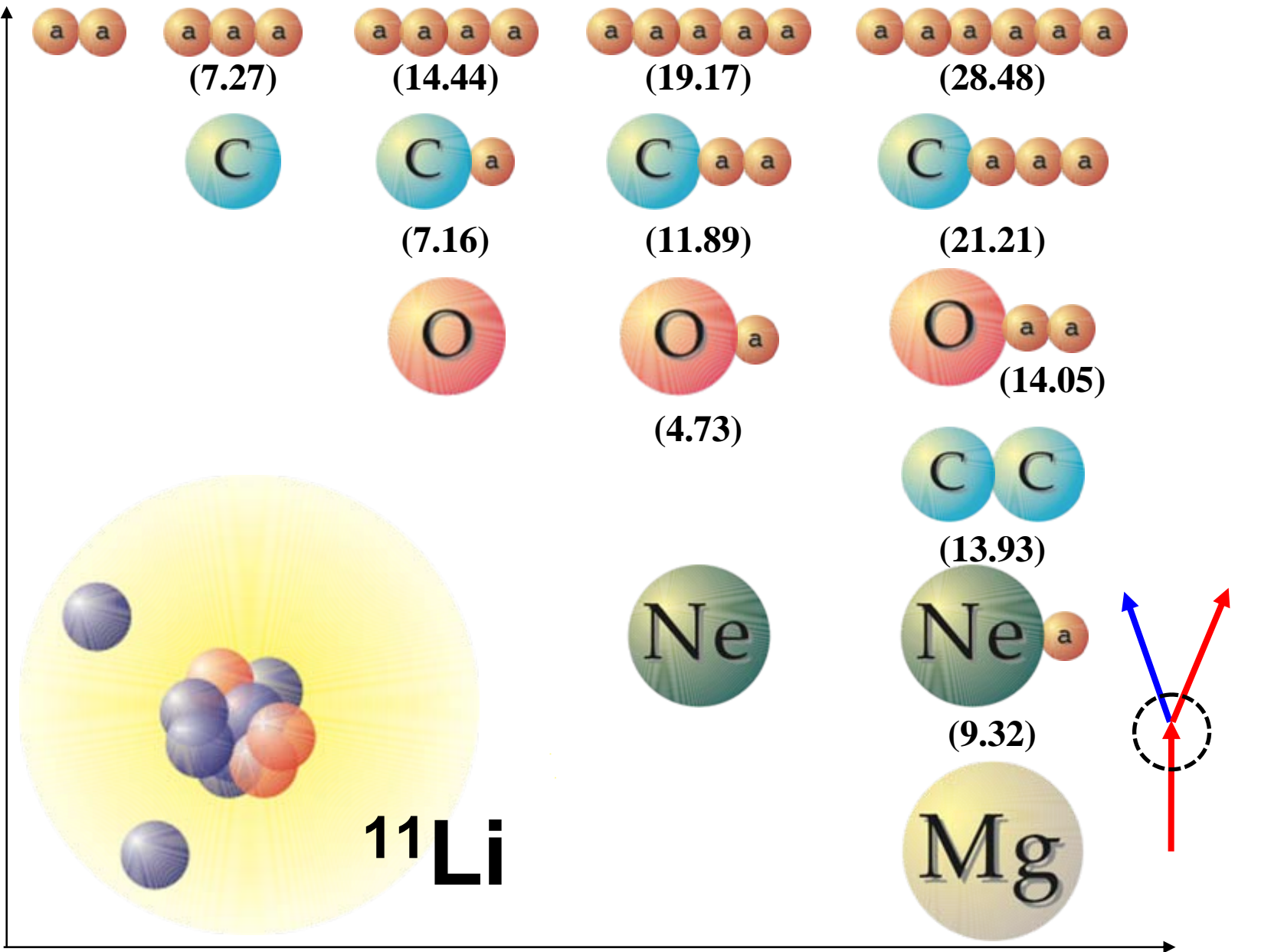


'Alignment' of w.b. state with the decay channel



Spectra and matter distribution modified by the proximity of scattering continuum

Excitation energy



¹¹Li

Mass number

threshold is a branching point

Coupling between analog states in (d,p) and (d,n)

C.F. Moore et al.
 Phys. Rev. Lett. 17, 926 (1966)

